Policy implications of the Bargaining Family

Akira Yakita Nanzan University

Abstract

We consider a two-stage family game in which women and men choose education levels in stage 1 and choose the amount of contribution to family public goods in stage 2. If they cannot commit themselves to decisions of the provision of family public goods, the stage-2 decision might be made through bargaining, say, Nash bargaining. That possibility affects the stage-1 decision. These analyses demonstrate that bargaining in stage 2 engenders under-provision of family public goods. To achieve an efficient level of family public goods, government must rely on policies related to education choices rather than those related to contribution decisions.

Keywords: Nash bargaining; family public goods; family policy JEL Classifications: D13; **H**42; J13; J24

Correspondence: Akira Yakita, Faculty of Economics, Nanzan University, 18 Yamasato-cho, Showa-ku, Nagoya 466-8673, Japan e-mail: yakita@nanzan-u.ac.jp

1. Introduction

This study analyzes the effects of strategic behaviors of individuals related to education and family public goods provision. Individuals in any society might be expected to behave cooperatively to maximize the future welfare of the society. Although this is true for decisions related to both premarital investment in human capital accumulation and the provision of family public goods after marriage, they might alter their behaviors to be strategic in providing family public goods such as child rearing. They might do so because investment in education is determined personally before marriage. They do not know who is a partner. However, after marriage, a woman and a man must share housework as a particular couple despite their potential inherent mutual differences. Spouses might wish to take advantage during bargaining related to family public goods provision between them. Therefore, without commitment, they must consider the possibility of bargaining even when choosing a level of investment in education before marriage. This paper presents an examination of the consequences of such a family bargaining game and compares its sequence with the efficient solution. The efficient solution is obtainable by unitary cooperation with commitment throughout stages before and after marriage.

The possibility of no commitment in family decision-making has been emphasized by Kemnitz and Thum (2015), who described that family decisions made cooperatively at earlier stages might be altered by changes in the relative bargaining power of women and men. Such a change in decision rules engenders time inconsistency issues related to family decision-making.¹ Konrad and Lommerud (2000) considered that human capital investment decisions might be made non-cooperatively, although daily life decisions related to family public goods might be made through bargaining between spouses.² Rasul (2008) used the Malaysia Family Life Survey to show that spouses bargain without commitment. If couples bargain without commitment, then the influence of each spouse's preference on fertility outcomes depends on the relevant threat point in

¹ Basu (2006) asserted that household decisions affect the distribution of bargaining power between genders, which in turn alters household decisions. Iyigun and Walsh (2007b) analyzed effects of the difference in the relative population sizes of women and men on education investments of each gender before marriage, assuming similar feedback effects on relative bargaining power.

 $^{^2}$ Lundberg and Pollak (1993) presented the first report of the relevant literature describing analysis of non-cooperative behaviors in a family other than divorce between spouses. Rainer (2008) extended Konrad and Lommerud (2000) by assuming that wives have a comparative advantage in the household activity to examine when and how couples can achieve effective outcomes in a self-enforcing manner.

marital bargaining, and the distribution of bargaining power. Mazzocco (2007) used US data to test intra-family commitment and concluded that non-commitment collective models might be appropriate for policy making.³ Without commitment, women (or wives) wish to supply labor to the market at a lower wage rate than with commitment in Kemnitz and Thum (2015), whereas women invest more in their human capital than in the efficient solution in Konrad and Lommerud (2000). In both studies, the change of the behavioral rule tends to lower family public goods provision.

We consider a two-stage game, i.e., before-marriage and after-marriage, as reported also by Konrad and Lommerud (2000). Women and men choose education levels unitarily in stage 1 and decide upon contributions to family public goods, for expositional simplicity, through Nash bargaining in stage 2. The main result is that the possibility of family bargaining related to public goods in stage 2 engenders over-investment in education. To achieve the efficient level of family public goods, government must rely on policies related to educational choices rather than on decisions of contributions. This result has important implications for family policies in developed countries with low fertility.

The game examined herein can be regarded as a supplement to the analysis described by Konrad and Lommerud (2000), who assumed non-cooperative education decisions in stage 1 and a Nash cooperative bargaining solution of family public goods provision in stage 2. The difference in games generates different policy implications. The next section introduces the model. Section 3 presents analysis of the two-stage game. Section 4 explains policy implications of the theoretical results. The last section concludes the paper.

2. Model

We assume a variation of the two-stage family decisions model described by Konrad and Lommerud (2000) by assuming a different game from theirs in stage 1. The other parts are the same as those described in Konrad and Lommerud (2000). Therefore, we make use of the same notation of variables unless it is necessary to distinguish them.

A family is assumed to consist of a woman and a man, i.e., a couple. Our main concern is the provision of family public goods in stage 2. Therefore, we assume equal sizes of women and men population to avoid the issue of matching individuals. The marriage matching process is also assumed to be exogenous. Each individual has a

³ Attanasio and Lechene (2002) tested and rejected the income pooling hypothesis using Progresa data of Mexico.

payoff function

$$u_i = c_i + G - a(g_i) - b(w_i).$$
(1)

Subscript *i* denotes the gender, i = f, m, where *f* and *m* represent female and male. *G* is the amount of family public goods, which is the sum of individual time contributions of the two, i.e.,

$$G = g_f + g_m. \tag{2}$$

Denoting the time endowment of a person by y, a person can allocate it between market labor, $y-g_i$, and the contribution to family public goods, g_i . Person *i*'s consumption is given as

$$c_i = (y - g_i)w_i, \tag{3}$$

where w_i denotes the person *i*'s market wage rate. The contribution to family public goods has a psychic cost that is measured using a strictly convex cost function $a(g_i)$, $a'(g_i) > 0$ and $a''(g_i) > 0$. Individuals also choose efforts on educational activities that increase their market wage rate. The effort to gain wage w_i is expressed as a strictly convex function $b(w_i)$, $b'(w_i) > 0$ and $b''(w_i) > 0$.

In stage 1 of our two-stage game, individuals simultaneously choose their education levels and thereby their wage rates. In stage 2, individuals know the choices of wage rates in stage 1 and simultaneously decide how long they devote to provision of family public goods. We assume that women and men jointly make education decisions, although they might not want to commit to the joint decision related to family public goods provision to be made in stage 2. A choice of education is often made before making up a family. Therefore, if persons wish to be happy during marital time, then their decision-making might be done unitarily because each person might not know who is a partner. Once they are married as a particular couple, however, there can be conflicts between them in the allocation of contributions to family public goods for given education choices.⁴ Chiappori et al. (2009) reported that women increased their market

⁴ We assume away biological gender differences in this paper for analytical simplicity.

work whereas men reduced their market work and increased their non-market work in the United States during 1975–2003. Women and men have come to behave similarly. Therefore, decisions related to contributions to family public goods (or market labor supply) might be regarded as the outcome of bargaining between spouses with equal bargaining power. For these analyses, we assume that the contribution decision is made through Nash bargaining.

We now solve such two-stage family problems backward. First, starting from a situation with given education choices of the couple (w_f, w_m) , we calculate a Nash

contribution equilibrium with no cooperation in stage 2. Because we are concerned with provision of family public goods, we assume here that couples do not legally divorce once they have married. Instead, they might divorce or separate within the home.⁵ The non-cooperative Nash equilibrium is taken as the threat point of a Nash cooperative bargaining solution.⁶ Next, we calculate the problem for a case in which both decisions related to the education and contribution choices are made unitarily within couples. This unitarily cooperative case provides an efficient solution by definition. Finally, assuming that family public goods provisions are renegotiated and bargained between spouses in stage 2, we examine the outcome of the Nash bargaining over provision of family public goods. Hereinafter, the game with unitary cooperation in both stages is called game C, whereas the game with unitary cooperation in stage 1 and Nash bargaining in stage 2 is called game NB. Therefore, the purpose of this paper can be redescribed as a comparison of the education and contribution and contribution levels in game C with those in game NB.⁷

3. Family decisions related to the contribution to public goods decisions

3.1 Contribution decisions in stage 2

In this section, for given education choices (w_f, w_m) , we first examine non-cooperative

Nash equilibrium, then unitary cooperation, and finally the Nash bargaining solution.

⁵ Lundberg and Pollak (1993) proposed a separate spheres model in which the threat point from which cooperative Nash bargaining proceeds is not divorce, but a non-cooperative equilibrium within marriage. Our assumption of Nash bargaining is similar to the notion of the separate sphere in their model.

⁶ Nash equilibrium does not necessarily mean a legal divorce because family public goods are commonly available to both once they are provided.

⁷ Game NB can be regarded as a correspondence to the "sequential decisions" in Kemnitz and Thum (2015).

The Nash equilibrium (g_f^*, g_m^*) is obtainable as follows. Equilibrium g_i^* maximizes

$$u_{i} = (y - g_{i})w_{i} + g_{i} + g_{j}^{*} - a(g_{i}) - b(w_{i})$$
(4)

for $g_i \in [0, y]$ (i, j = f, m and $i \neq j$). Given the convexity of $a(g_i)$, the contribution can be determined uniquely. Assuming an interior solution, the equilibrium contribution is obtained using the first-order condition

$$-w_i + 1 - a'(g_i^*) = 0.$$
⁽⁵⁾

From (5) we obtain

$$g_i^*' = \frac{dg_i^*}{dw_i} = -\frac{1}{a''(g_i^*)} < 0.$$
(6)

The sign of (6) is obtainable from the convexity of $a(g_i)$. The Nash-equilibrium utility

levels in the stage-2 non-cooperative game are denoted as $u_i^* = u_i(g_f^*, g_m^*)$.

Next, we analyze the unitary cooperation in stage 2 for given (w_f, w_m) . The game in stage 1 is also unitarily cooperative. Therefore, the solution gives the efficiency outcome. We assume that monetary and utility transfers between family members are allowed. The cooperative levels of contribution for public goods (g_f^e, g_m^e) are determined by the first-order conditions as

$$-w_f + 2 - a'(g_f^e) = -w_m + 2 - a'(g_m^e) = 0.$$
⁽⁷⁾

Here we assume an interior solution. From the convexity of $a(g_i)$, the contributions are determined uniquely; they satisfy $g_i^e = dg_i^e / dw_i = -1/a''(g_i^e) < 0$. From (5) and (7), it follows that $g_i^e(w_i) > g_i^*(w_i)$.

We now turn to the Nash bargaining solution in stage 2, where the threat point is given as (u_f^*, u_m^*) . We assume that monetary side-payments can be made between the

family members. Because efficiency contributions of g_f^e and g_m^e depend respectively only on w_f and w_m , the utility possibility frontier is $u_f = V - u_m$, with

$$V = u_f(g_f^e, g_m^e) + u_m(g_f^e, g_m^e)$$

= $\sum_{i \in (f,m)} [(y - g_i^e)w_i - a(g_i^e) - b(w_i)] + 2(g_f^e + g_m^e).$ (8)

The utility possibility frontier is linear with slope of negative one. The Nash bargaining solution brings about utilities⁸

$$u_i^{NB} = \frac{V}{2} + \frac{u_i^* - u_j^*}{2} \text{ for } i, j = f, m \text{ and } i \neq j.$$
(9)

3.2 Educational decisions in stage 1

Next we examine the choices on education levels in stage 1 when the provision of family public goods is chosen through Nash bargaining in stage 2. To compare the non-commitment solution with the efficient solution, we examine the case in which decisions about contributions to family public goods are also made unitarily in stage 2 because educational choice depends on whether stage 2 is characterized by unitary cooperation or by Nash bargaining.

First, we consider the case with unitary cooperation in stage 2, hereinafter called game C, which leads to an efficient solution. Individual *i*'s problem is to choose a wage rate w_i that maximizes

$$\sum_{i \in (f,m)} [(y - g_i^e)w_i - a(g_i^e) - b(w_i)] + 2(g_f^e + g_m^e),$$
(8)

where $g_i^e(w_i)$ is determined in (7). The first-order condition is

$$y - g_i^e(w_i^C) - b'(w_i^C) = 0.$$
⁽¹⁰⁾

In deriving (10), we used (7).

Next, we consider the case of Nash bargaining within the family in stage 2. The

⁸ The solution can be obtained by maximizing $(u_f - u_f^*)(u_m - u_m^*)$ subject to the utility possibility frontier.

game is called game NB. Because individuals are symmetrical in this paper, the equilibrium wage rate of individual i can be formalized as the choice of w_i that maximizes⁹

$$u_{i}^{NB} = \frac{1}{2} \{ \sum_{i \in (f,m)} [(y - g_{i}^{e})w_{i} - a(g_{i}^{e}) - b(w_{i})] + 2(g_{f}^{e} + g_{m}^{e}) + [(y - g_{f}^{*})w_{f} + g_{f}^{*} + g_{f}^{*} - a(g_{f}^{*}) - b(w_{f})] - [(y - g_{m}^{*})w_{m} + g_{f}^{*} + g_{m}^{*} - a(g_{m}^{*}) - b(w_{m})] \}.$$
(11)

The first-order condition is

$$y - g_f^*(w_f^{NB}) - b'(w_f^{NB}) - g_f^*'(w_f^{NB}) = 0, \qquad (12)$$

where we use (5) and (7). The last term on the right-hand side of (12) represents the redistribution according to the Nash bargaining game. Because of the increased wage rate, the individual will marginally change her contribution to household public goods production by $g_f^*(w_f)$. This change in turn reduces the male's utility by the same amount.

Now we compare the education level in game NB with that in game C. Differentiating (11) with respect to w_f and evaluating at w_f^C , we obtain

$$\frac{\partial u_f^{NB}}{\partial w_f} = \frac{1}{2} [y - g_f^*(w_f^C) - b'(w_f^C) - g_f^*'(w_f^C)].$$
(13)

Therefore, we have¹⁰

$$w_f^{NB} \stackrel{>}{\underset{<}{=}} w_f^C$$
 as $\frac{\partial u_f^{NB}}{\partial w_f} \stackrel{>}{\underset{<}{=}} 0$. (14)

Because $b'(w_f^C) = y - g_f^e(w_f^C)$ from (10), we can rewrite (13) as

⁹ If asymmetry between genders is assumed, then the analysis is more complicated. Rainer (2008) specifically addressed the differences in ability between genders.

¹⁰ Function u_i is a concave function of w_i .

$$\frac{\partial u_f^{NB}}{\partial w_f} \bigg|_{w_f = w_f^C} = \frac{1}{2} [g_f^e(w_f^C) - g_f^*(w_f^C) - g_f^*'(w_f^C)].$$
(15)

Because $g_i^e(w_i) - g_i^*(w_i) > 0$ and $g_i'(w_i) < 0$, it follows that $\partial u_f^{NB} / \partial w_f \Big|_{w_f = w_f^C} > 0$

and that we therefore have $w_f^{NB} > w_f^C$, which leads to the following proposition.

PROPOSITION 1. Presuming that the educational decision in stage 1 is chosen unitarily and that contributions to family public goods are bargained cooperatively between women and men. Education levels are always higher than those that would be obtained by unitary cooperation in both stages.

It is noteworthy that the education level in game NB is higher than the education level in game C, irrespective of whether the function $a'(g_i)$ is convex or concave.

Nash bargaining between spouses in stage 2 invariably results in overinvestment in education. In Konrad and Lommerud (2000), whether the education level chosen in Nash bargaining of stage 2 with the education level determined non-cooperatively in stage 1 is greater than, equal to, or less than that obtained in Nash equilibrium depends on the characteristic of function a'(g). In contrast, in this paper, the education level determined with family bargaining related to public goods is *always* greater than that with the unitarily chosen family public goods.

The first two terms in the bracket on the right-hand side of (15) represent the efficiency effect. An increase in the wage rate increases the family income and, consequently, family public goods through the income effect. The last term is the distribution effect, as described above. The increased education level lowers the marginal provision of public goods of the wife, which increases her utility but which lowers her husband's utility by the same amount in the Nash bargaining. In this case of symmetric individuals, additional education at the efficiency level raises the utility of

each in Nash bargaining. Because
$$g_i'(w_i) < 0$$
 , we have

 $g_i^{NB} = g_i(w_i^{NB}) < g_i^C = g_i(w_i^C)$.¹¹ The level of family public goods in game NB is

¹¹ Assuming interior solutions, we have $g_i^{NB}(w_i) = g_i^C(w_i)$ because (5) holds for both

lower than that in game C. g_i^C is obtainable by unitary cooperation at both stages. Therefore, Nash bargaining in stage 2 renders the level of family public goods provision lower than in the efficient solution.

3.3 Policy implications for fertility

The previous subsection shows that Nash bargaining in stage 2 affects the choice of education levels in stage 1. Child rearing can be regarded as a family public good. Therefore, the number of children might depend on the total contribution to family public goods.¹² Following Galor and Weil (1996), the number of children is proportional to the time spent by parents, i.e., $n = (g_f + g_m)/z \equiv v(g_f + g_m)$, where *n* denotes

the number of children in the family and z is the cost in time of raising one child.¹³ With Nash bargaining in stage 2, the chosen number of children is smaller than that obtained under the efficient solution. In the literature related to family economics, it is often suggested that governments of nations that are affected by low fertility should pursue some family policy such as a child allowance or child-care policy. Governments have actually implemented such policies in many countries (see, for example, Luci-Greulich and Thévenon, 2013). The theoretical result obtained in the previous section implies that, if fertility decisions are made by family bargaining, then education policy rather than family policy is necessary to increase the number of children and thereby increase the fertility rate.

In this section, to examine policy implications for family decisions, we analyze the effects of changes in education and family policies, which influence a threat point of

¹³ In this case, representing children n as family public goods, the payoff of individual can be written as $u_i = (y - g_i)w_i + v(g_f + g_m) - a(g_i) - b(w_i)$. For analytical simplicity, we assume away inherent gender differences in the roles of raising children between women and men in this paper. Although only mothers can actually generate

games C and NB.

¹² Although Iyigun and Walsh (2007a) emphasized a biological difference between genders, Gupta and Smith (2002) reported that there is no indication that rearing children had any long-term negative effects on the earning potential of their mothers in Denmark during 1980–1995. If child-rearing has no effect on mothers earning potentials, the absence of mothers' specific contributions to child-rearing might be negligible in formulating lifetime earnings.

between women and men in this paper. Although only mothers can actually generate children, both spouses can provide internal child care even in the event of divorce within the home, i.e., at the threat point of this game. Though, even with respect to legal divorce, Alesina and Giuliano (2006) among others reported that the introduction of unilateral divorce does not seem to affect total marital fertility by encouraging women planning to have children marry more easily.

Nash bargaining in stage 2.^{14,15}

For instance, presuming that a subsidy in support of contributions to family public goods at rate s is financed through lump-sum taxes on individuals, then the terms in the brackets on the right-hand side of (15) become

$$g_{f}^{e}(w_{f}^{C}) - g_{f}^{*}(w_{f}^{C}) - (1+s)g_{f}^{*}'(w_{f}^{C}) > 0.$$
(16)

The subsidy might increase the difference between education levels in game C and NB. Therefore, family policy related to child-bearing cannot alleviate inefficiency in fertility decisions by itself. This result is in contrast to the result of Boadway et al. (1989) and Konrad and Lommerud (1995), who argued that lump-sum-tax-financed subsidies for the public goods reduce the under-provision problem by increasing the incentives for private provision of the public goods. The difference from us mainly stems from endogenous education investment at stage 1 in our model. The subsidy policy rather deteriorates the inefficiency issue by affecting a threat point for cooperative bargaining.¹⁶

To increase the fertility rate, therefore, the government must rely on education policy even if educational decisions are made through unitary cooperation in stage 1. A government might impose a tax on education investment in the situation of Nash bargaining of game NB, although taxes are not imposed in the case of unitary cooperation over two stages. In this case, the terms in the brackets on the right-hand side of (15) is

$$[g_{f}^{e}(w_{f}^{C}) - g_{f}^{*}(w_{f}^{C}) - g_{f}^{*}'(w_{f}^{C})] - \tau[y - g_{f}^{e}(w_{f}^{C})].$$
(17)

The second term on the right-hand side of (17) is negative. The first term is positive. The tax policy can alleviate the inefficiency issue by shifting a threat point. Therefore, the tax might achieve the efficiency education level under certain conditions. If the policy reduces the education levels of individuals in stage 1 to the efficient level, then

¹⁴ Konrad and Lommerud (1995) point out that if the non-cooperative equilibrium only serves as a threat point for cooperative bargaining outcomes, it matters for the impact of a policy who would gain more in the non-cooperative equilibrium from the shift in the threat point due to the policy.

¹⁵ We assume that government can commit to implementing tax/subsidy these policies certainly, i.e., government is not a player of the Nash equilibrium game. Basu (2011) might doubt such an assumption.

¹⁶ Because of the lack of observability of childcare activities, Konrad and Lommerud (1995) regard the labor income tax as a second-best policy. However, they also report that it is when there is no third activity for which time can be used, e.g., leisure, that a lump-sum redistribution tax on labor income has the same effect.

public goods provisions might increase toward the efficiency level.¹⁷

PROPOSITION 2. Presuming that the education decision in stage 1 is done efficiently and assuming that the contributions to family public goods are negotiated cooperatively between women and men. A positive tax on education expenditure might achieve the efficient level of family public goods provision.

The intuition behind the results is the following: Subsidies for provision of public goods are expected to induce both spouses to increase public goods supply by lowering the cost of public goods provision. Therefore, each spouse is likely to increase education expenditure to take an advantage over the other spouse in bargaining rather than to increase the contribution to family public goods. Taxes on education expenditure induce each individual to reduce the expenditure because of higher costs. The lowered education expenditure increases the level of public goods provision in Nash equilibrium as a threat point for cooperative Nash bargaining.

Although the policy arguments resemble those presented by Konrad and Lommerud (2000), the tax policy might not be used in their case, assuming Nash equilibrium in stage 1 because whether over-investment or under-investment occurs depends on the curvature of function a'(g). In contrast, the tax on education investment must be positive because of excessive education investment in the case of game NB. Nevertheless, it is noteworthy that our result does not mean that investment in education must always be taxed. It is the case only when the chosen investment level is higher than the efficient solution level. Without commitment, spouses want to obtain advantageous benefits in bargaining family public goods provision by bearing additional efficiency costs of excessive education activities.

4. Conclusion

We have presented an examination of a two-stage game of unitary cooperation in stage 1 and Nash bargaining in stage 2; then it was compared with the educational and contribution-to-family public-goods decisions with the efficient solution. This game was not analyzed in a study reported by Konrad and Lommerud (2000). The results presented in the present paper therefore complement their results. The Nash-bargained contributions to family public goods are lower than those under the efficient solution. The education levels obtained through Nash bargaining in stage 2 are higher than those

¹⁷ For derivation, see Appendix.

of the efficient solution in both stages.

The main message presented in this paper is the following. We might consider a case in which the provision of family public goods such as child rearing at home is determined without *ex ante* commitment, although education decisions are made through unitary cooperation, i.e., efficiently. We instead assume Nash bargaining in stage 2. In our case, the level of family public goods chosen will be lower than that of the efficient solution. The policy related to the education decisions, but not to the contribution-to-family public-goods decisions, should be undertaken to increase the number of children and the fertility rate.

From the analysis described in this paper, the fertility rebounds observed in developed countries might be interpreted as a consequence of possible shifts from family bargaining to unitary cooperation between spouses, i.e., a change to unitary cooperation. ¹⁸ Actually, gender-equality policies have recently been adopted in developed countries (Olivetti and Petrongolo, 2017).¹⁹ If the economic situations of spouses become equal, then cooperation rather than bargaining might be plausible.²⁰ Next, although Chiappori et al. (2009) reported that the gender gaps in the amount of time spent in non-market work declined during 1975–2003, significant gender wage gaps persist, but educational levels of women are higher than those of men in several developed countries. This gender twist between wage rates and education levels might affect individuals' decisions on education and fertility.²¹ This issue is left as a subject of future research.

Appendix: Proof of Proposition 2

We consider the effects of policies on education investment in game NB. First, we consider a subsidy in relation to children. It is not possible to grasp psychic costs for

¹⁸ Myrskylä et al. (2009) demonstrated that the relation between the total fertility rate and the human development index (HDI) changed from negative to positive using long-term data of more than 100 countries.

¹⁹ The French government introduced fathers' paid child-care leave in 2002, but in Sweden, child-care leave has been compensated with income transfers since 2007. The Swedish government started to award bonuses if parents take child-care leave equally in 2008. As Rainer (2008) concluded, sharing rules such as "equal sharing" can be maintained when women and men have equal opportunities in the labor market. Marriage might not be formal or legal in many economically developed countries.

²⁰ However, if contributions to family public goods are bargained even with paid leaves for both spouses, over-investments in education might still be a result.

²¹ Morita and Yakita (2016) examined the relation between fertility and gender wage gaps. Day also provides relevant information (2012).

policy purposes. Therefore, we consider subsidies to family public goods provision g_i at rate s:

$$u_i^{NB} = \frac{1}{2} \{ \sum_{i \in (f,m)} [(y - g_i^e)w_i - a(g_i^e) - b(w_i)] + 2(g_f^e + g_m^e) + [(y - g_f^*)w_f + (1 + s)(g_f^* + g_f^*) - a(g_f^*) - b(w_f) - T] - [(y - g_m^*)w_m + (1 + s)(g_f^* + g_m^*) - a(g_m^*) - b(w_m) - T] \},$$
(11)

where T is a lump-sum tax. Individuals know that family public goods provision is subsidized only in Nash bargaining case, i.e., at the threat point. From maximization of

 u_i^{NB} , we obtain (16).

Next, if a tax is imposed on education investment at rate τ , then the education decision in game NB is obtainable from maximizing

$$u_i^{NB} = \frac{1}{2} \{ \sum_{i \in (f,m)} [(y - g_i^e)w_i - a(g_i^e) - b(w_i)] + 2(g_f^e + g_m^e) + [(y - g_f^*)w_f + g_f^* + g_f^* - a(g_f^*) - (1 + \tau)b(w_f) + B] - [(y - g_m^*)w_m + g_f^* + g_m^* - a(g_m^*) - (1 + \tau)b(w_m) + B] \}$$
(11")

for w_f , where B denotes lump-sum transfers from the government. Individuals are assumed to know that education investment is taxed only in Nash bargaining, i.e., at the threat point. From the first-order condition and evaluating at w_f^e , we obtain

$$\frac{\partial 2u_f^{NB}}{\partial w_f} = [g_f^e(w_f) - g_f^*(w_f) - g_f^*'(w_f)] - \tau[y - g_f^e(w_f)].$$
(17)

The second term on the right-hand side of (17°) is negative. The first term is positive. Therefore, the tax might achieve the efficiency education level under certain conditions. In that case, the optimal tax rate is given by setting (17°) equal to zero as

$$\tau = \frac{g_f^e(w_f^e) - g_f^*(w_f^e) - g_f^*'(w_f^e)}{y - g_f^e(w_f^e)} > 0.$$
(A1)

If the tax rate is less than one, then a tax policy would not achieve efficiency. Because individuals are symmetric, the same argument is applicable to men. Therefore, $w_i^{NB} = w_i^e$ with such a tax. When the education level is efficient, the level of family public goods is also efficient, i.e., $g_i(w_i^{NB}) = g_i(w_i^e)$. References

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